# WESTMINSTER INTERNATIONAL UNIVERSITY IN TASHKENT

## Cambridge A Level MATHEMATICS ENTRANCE TEST

#### CANDIDATE NAME

#### CANDIDATE ID NUMBER

## 19th of August 2022

1 hour 30 minutes

You must answer on the question paper.

You will need: Geometrical instruments

### **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For  $\pi$  use 3.14.

#### **INFORMATION**

- The total mark for this paper is 100.
- The number of marks for each question or part question is shown in brackets [].

## FOR OFFICE USE ONLY.

1.	2.	3.	4.	5.	6.	7.	8.	9.	10.	Total

#### This document has 20 pages. Any blank pages are indicated.

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## ANSWER WITHOUT THE CORRECT AND FULL SOLUTIONS WILL NOT BE MARKED. PROVIDE THE DETAILED SOLUTION AND GIVE THE CORRECT ANSWER ON THE PROVIDED SPACE BELOW. THERE IS NO MARK FOR PARTIAL ANSWERS.

### 1 [12m] (a) In October, Sara is charged \$84.25 for water. A tax of 8% is added to this amount. Calculate the total amount Sara is charged for water in October including tax.

\$.....[2]

(b) The table shows the rates that Sara is charged for her gas and electricity supply. She is charged a fixed amount each day plus an amount for each unit used.

	Cost for one day	Cost for one unit			
Gas	23 cents	4.3 cents			
Electricity	28 cents	16 cents			

(i) Sara uses a total of 960 units of gas in the 30 days of November.Calculate the total amount, in dollars, Sara is charged for gas in November.

\$ .....[2]

(ii) Sara is charged a total of \$30.80 for electricity in the 30 days of November. Calculate the number of units of electricity she used.

(c) The amount of electricity generated is measured in Gigawatt hours (GWh).

The table shows information about the amount of electricity generated in different countries.

Country	Electricity generated in 2010 (GWh)	Electricity generated in 2016 (GWh)
Australia	$2.37  imes 10^5$	$2.43  imes 10^5$
Japan	$1.09  imes 10^6$	$1.03  imes 10^6$
Spain	$2.91  imes 10^5$	$2.64  imes 10^5$
Turkey	$2.03  imes 10^5$	$2.62 \times 10^{5}$

(i) Calculate how much more electricity was generated in Japan than in Australia in 2016. Give your answer in standard form.

..... GWh [1]

(ii) Calculate the percentage increase in electricity generated in Turkey from 2010 to 2016.

.....% [2]

(iii) There was a 4% decrease in the amount of electricity generated in Spain from 2013 to 2016.Calculate the amount of electricity generated in Spain in 2013.

...... GWh [2]

**2** [9m] **(a)** The table shows the number of exercise classes attended in one week by each of 80 members of a gym.

Number of classes	0	1	2	3	4	5
Frequency	10	29	26	10	3	2

(i) Find the mode.

(ii) Find the median.

.....[1]

.....[1]

(iii) A pie chart is drawn to show this information. Calculate the angle representing 5 classes attended.

.....[2]

(b) Some members of the gym were surveyed about how much time they spent at the gym. The histogram shows the times, t minutes, they spent on their last visit.



(i) Thirty members spent between 30 and 60 minutes at the gym. Calculate the number of members surveyed.

.....[3]

(ii) Ravshan says: One tenth of these members spent longer than  $1\frac{1}{2}$  hours at the gym on their last visit. Is he correct? Justify your answer.

......[2]



NOT TO SCALE

Points *A*, *B* and *C* are on the circle, centre *O*. *AOC* and *OBE* are straight lines. *DE* is a tangent to the circle at *C*. *ABO* =  $34^{\circ}$ 

(i) Explain why triangle *AOB* is isosceles.

.....[1]

(ii) Find  $\angle BEC$ .



*OPS* and *OQR* are sectors of circles each with centre *O*. *OPQ* and *OSR* are straight lines. OP = 7.4 cm, PQ = 1.2 cm and  $QOR = 96^{\circ}$ Calculate the shaded area.

..... cm<sup>2</sup> [3]

**4** [10m] (a)



The diagram shows the positions of three villages, *P*, *Q* and *R*. *R* is due west of *P* and *Q* is on a bearing of 140° from *P*. PR = 3.8 km and QR = 7.5 km.

(i) Calculate angle *PRQ*.

(ii) Work out the bearing of R from Q.

(b) The distance by road from village P to village T is 16.5 km.

Komiljon leaves village P at 10 30 and drives to village T at an average speed of 45 km/h. He stops in village T for 15 minutes. He then drives back to village P and arrives there at 11 35.

Calculate Komiljon's average speed, in km/h, for the journey back from village *T* to village *P*.

..... km/h [4]

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5 [8m] (a)
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Kholida has these 10 number cards. She takes a card at random, notes the number and replaces it. She then takes a second card.

(i) Find the probability that the first card Kholida takes shows an even number.



(iii) Work out the probability that Kholida takes one odd number and one even number.

(b) Basma has a bag containing 5 yellow counters, 3 pink counters and 4 black counters. She takes two counters from the bag at random, without replacement. Find the probability that she takes one yellow counter and one pink counter.

Give your answer as a fraction in its simplest form.

.....[3]

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**6** [12m] (a)



The diagram shows a right-angled triangle, with dimensions given in centimeters.

(i) Show that  $5x^2 + 30x - 39 = 0$ .

(ii) Solve the equation  $5x^2 + 30x - 39 = 0$ . Show your working and give your answers correct to 2 decimal places.

 $x = \dots$  [3]

[3]

(iii) Calculate the area of the triangle.

..... cm<sup>2</sup> [2]



The diagram shows a different right-angled triangle. The length of the hypotenuse is 12 cm.

Calculate the shortest distance from A to BC.

..... cm [4]



The line 2y = x is drawn on the grid.

(a) On the grid, draw the graph of

(i) 
$$y = 2$$
 [2]

(ii) 
$$y + x = 4$$
 [3]

- (b) On the grid, shade and label the region R, defined by the following inequalities.
  - $x + y \le 4 \qquad \qquad 2y \ge x \qquad y \le 2 \qquad \qquad x \ge 0 \qquad \qquad [6]$

- **8** [7m] *A* is the point (-2, 3) and *B* is the point (4, 5).
  - (a) Find the coordinates of the midpoint of *AB*.

(b) Show that the equation of line AB is 3y = x + 11.

(.....)[1]

(c) Find the equation of the perpendicular bisector of line AB.

[3]

.....[3]

**9** [12m] (a) Solve 3x - 8 = 7.

(b) Solve the inequality 7x < 3(2 - x).

.....[2]

*x* =.....[2]

(c) Solve  $\frac{3}{x-2} + \frac{x}{x+5} = 1$ .

*x* =.....[4]

(d) Simplify  $\frac{2x^2+3x+4xy+6y}{2x^2+11x+12}$ .

.....[4]

10 [12m] (a)

The diagram shows an isosceles triangle ABC where AB = AC.

D is a point on AC such that angle  $ADB = 90^{\circ}$ .

E is a point on AB such that angle  $AEC = 90^{\circ}$ .

Show that triangles ADB and AEC are congruent.

Give a reason for each statement you make.





**(b)** 



The diagram shows trapezium *ABCD*. AB = 7 cm and DC = 10 cm.

The area of *ABCD* is  $85cm^2$ .

The perpendicular height of the trapezium is h cm.

Find the value of h.

 $h = \dots$ [2]



Triangles A, B and C are drawn on the grid.

(i) Describe fully the single transformation that maps triangle A onto triangle B.

.....[2]

(ii) Describe fully the single transformation that maps triangle A onto triangle C.

.....[2]

(iii) Triangle D is the image of triangle A after an enlargement, scale factor 2, with centre of enlargement (1, 2).

Draw triangle D.

[3]

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